

Old Exam Questions – Old Course  
**Logarithms**

(C2 Winter 2005)

2. Use the substitution  $3^x = u$  to solve the equation

$$3^{2x} - 3^{x+2} + 14 = 0,$$

giving your answers correct to three decimal places. [6]

10. (a) Show that if  $x > 0$ ,

$$\log_a x^k = k \log_a x. \quad [3]$$

- (b) Solve the equation

$$\log_{10} (x^2 + 48) = \log_{10} x + 2\log_{10} 4. \quad [5]$$

(C2 Summer 2005)

6. (a) Given that  $x > 0, y > 0$ , show that

$$\log_a \left( \frac{x}{y} \right) = \log_a x - \log_a y. \quad [3]$$

- (b) (i) Solve the equation

$$5^{2x+1} = 7,$$

giving your answer correct to four decimal places.

- (ii) Express  $\log_{10} 2 + 2\log_{10} 18 - \frac{3}{2}\log_{10} 36$  as a single logarithm in its simplest form. [8]

(C2 Winter 2006)

10. (a) Given that  $x > 0, y > 0$ , show that

$$\log_a (xy) = \log_a x + \log_a y. \quad [3]$$

- (b) Given that  $\int_1^3 \log_{10} x \, dx$  has an approximate value of 0.5628, find an approximate value for  $\int_1^3 \log_{10} (10x) \, dx$ . Give your answer correct to four decimal places. [4]

(C2 Summer 2006)

8. (a) Given that  $x > 0$ , show that

$$\log_a(x^n) = n \log_a x. \quad [3]$$

- (b) Solve the equation

$$5^{3x+1} = 6,$$

giving your answer correct to four decimal places.

[4]

(C2 Winter 2007)

8. (a) Given that  $x > 0$ ,  $y > 0$ , show that  $\log_a(xy) = \log_a x + \log_a y$ .

[3]

- (b) Express  $\log_a 36 + \frac{1}{2} \log_a 256 - 2 \log_a 48$  as a single logarithm.

[4]

- (c) Solve the equation

$$2^{x+1} = 5,$$

giving your answer correct to three decimal places.

[2]

(C2 Summer 2007)

7. (a) (i) Given that  $p > 0$ ,  $q > 0$ , show that  $\log_a pq = \log_a p + \log_a q$ .

- (ii) Given that

$$\log_a x + \log_a (3x + 4) = 2 \log_a (3x - 4), \text{ where } x > \frac{4}{3},$$

find the value of  $x$ .

[8]

- (b) Solve  $3^x = 11$ , giving your answer correct to three decimal places.

[2]

(C2 Winter 2008)

6. (a) Given that  $x > 0$ ,  $y > 0$ , show that

$$\log_a \frac{x}{y} = \log_a x - \log_a y. \quad [3]$$

- (b) (i) Solve the equation

$$3^{2x-1} = 11,$$

giving your answer correct to three decimal places.

- (ii) Express  $\frac{3}{2} \log_a 16 + \log_a 6 - 2 \log_a 12$  as a single logarithm in its simplest form.

[7]

(C2 Summer 2008)

7. (a) Given that
- $x > 0$
- , show that

$$\log_a x^n = n \log_a x . \quad [3]$$

- (b) Solve the equation

$$\log_a(3x + 4) - \log_a x = 3 \log_a 2 . \quad [4]$$

- (c) Solve the equation

$$4^{3y+2} = 7 ,$$

giving your answer correct to three decimal places. [3]

(C2 Winter 2009)

7. (a) Given that
- $x > 0, y > 0$
- , show that

$$\log_a xy = \log_a x + \log_a y. \quad [3]$$

- (b) Solve the equation

$$\log_9 x = -\frac{1}{2} . \quad [2]$$

- (c) Solve the equation

$$\log_a(4x + 7) = \log_a x + 2 \log_a 3. \quad [4]$$

(C2 Summer 2009)

7. (a) Given that
- $x > 0, y > 0$
- , show that

$$\log_a \frac{x}{y} = \log_a x - \log_a y. \quad [3]$$

- (b) Solve the equation

$$3^{5-2x} = 7.$$

Show your working and give your answer correct to three decimal places. [3]

- (c) Solve the equation

$$\log_a(x - 3) + \log_a(x + 3) = 2 \log_a(x - 2). \quad [4]$$

(C2 Winter 2010)

7. (a) Given that
- $x > 0$
- , show that

$$\log_a x^n = n \log_a x. \quad [3]$$

- (b) Express
- $\frac{1}{2} \log_a 324 + \log_a 56 - 2 \log_a 12$
- in the form
- $\log_a b$
- , where
- $b$
- is a constant whose value is to be found. [4]

- (c) (i) Rewrite the equation

$$3^x = 2^{x+1}$$

in the form

$$c^x = d,$$

where the values of the constants  $c$  and  $d$  are to be found.

- (ii) Hence or otherwise, solve the equation

$$3^x = 2^{x+1},$$

giving your answer correct to two decimal places. [4]

(C2 Summer 2010)

8. (a) Given that
- $x > 0$
- , show that

$$\log_a x^n = n \log_a x. \quad [3]$$

- (b) Solve the equation

$$6^{2y-1} = 4.$$

Show your working and give your answer correct to three decimal places. [3]

- (c) Given that
- $\log_a 4 = \frac{1}{2}$
- , find the value of
- $a$
- . [2]

(C2 Winter 2011)

7. Find all values of
- $x$
- satisfying the equation

$$\log_a (6x^2 + 11) - \log_a x = 2 \log_a 5. \quad [5]$$

(C2 Summer 2011)

7. (a) Given that
- $x > 0$
- ,
- $y > 0$
- , show that

$$\log_a \left( \frac{x}{y} \right) = \log_a x - \log_a y. \quad [3]$$

- (b) Express

$$\frac{1}{2} \log_a x^8 - \log_a 4x + 3 \log_a \frac{2}{x}$$

as a single logarithm in its simplest form. [4]

(C2 Winter 2012)

7. (a) Given that
- $x > 0, y > 0$
- , show that

$$\log_a xy = \log_a x + \log_a y. \quad [3]$$

- (b) Solve the equation

$$2^{3-5x} = 12.$$

Show your working and give your answer correct to three decimal places. [3]

- (c) (i) Express

$$\log_9(3x - 1) + \log_9(x + 4) - 2\log_9(x + 1)$$

as a single logarithm.

- (ii) Hence solve the equation

$$\log_9(3x - 1) + \log_9(x + 4) - 2\log_9(x + 1) = \frac{1}{2}. \quad [5]$$

(C2 Summer 2012)

7. (a) Given that
- $x > 0$
- , show that

$$\log_a x^n = n \log_a x. \quad [3]$$

- (b) Solve the equation

$$9^{\frac{x}{2}-3} = 6.$$

Show your working and give your answer correct to three decimal places. [3]

- (c) Solve the equation

$$\log_a(x - 2) + \log_a(4x + 1) = 2\log_a(2x - 3). \quad [4]$$

(C2 Winter 2013)

7. (a) Given that
- $x > 0, y > 0$
- , show that

$$\log_a \frac{x}{y} = \log_a x - \log_a y. \quad [3]$$

- (b) Solve the equation

$$6^{2x+5} = 7.$$

Show your working and give your answer correct to three decimal places. [3]

(C2 Summer 2013)

7. (a) Given that
- $x > 0$
- ,
- $y > 0$
- , show that

$$\log_a xy = \log_a x + \log_a y. \quad [3]$$

- (b) Solve the equation

$$5^{2-3x} = 8.$$

Show your working and give your answer correct to three decimal places. [3]

- (c) Solve the equation

$$\log_a 90x^2 - \log_a \left(\frac{5}{x}\right) = \frac{1}{2} \log_a 144x^8. \quad [4]$$

(C2 Winter 2014)

7. (a) Given that
- $x > 0$
- , show that

$$\log_a x^n = n \log_a x. \quad [3]$$

- (b) Solve the equation

$$7^{5-4x} = 11.$$

Show your working and give your answer correct to three decimal places. [3]

- (c) Solve the equation

$$\log_8 x = -\frac{1}{3}. \quad [2]$$

(C2 Summer 2014)

7. (a) Solve the equation

$$3^{\frac{5x}{4}-2} = 7.$$

Show your working and give your answer correct to three decimal places. [3]

- (b) The positive numbers
- $a$
- and
- $b$
- are such that

$$\log_a b = 5.$$

- (i) Express
- $b$
- as a power of
- $a$
- .

- (ii)
- Using your answer to part (i)**
- , evaluate
- $\log_b a$
- . [3]

(C2 Summer 2015)

7. (a) Given that
- $x > 0$
- ,
- $y > 0$
- , show that

$$\log_a \left(\frac{x}{y}\right) = \log_a x - \log_a y. \quad [3]$$

- (b) Find all values of
- $x$
- satisfying the equation

$$\log_a(6x^2 + 9x + 2) - \log_a x = 4 \log_a 2. \quad [5]$$

(C2 Summer 2016)

7. (a) Given that
- $x > 0$
- , show that

$$\log_a x^n = n \log_a x. \quad [3]$$

- (b) Solve the equation

$$4^{3x+1} = 22.$$

Show your working and give your answer correct to two decimal places. [3]

- (c) Given that

$$\log_d z = 2\log_d 6 - \log_d 9 - 1,$$

express  $z$  in terms of  $d$ , giving your answer in a form **not** involving logarithms. [4]

(C2 Summer 2017)

7. (a) Given that
- $x > 0$
- ,
- $y > 0$
- , show that

$$\log_a \left( \frac{x}{y} \right) = \log_a x - \log_a y. \quad [3]$$

- (b) Express

$$\frac{1}{3} \log_b x^{15} - \log_b 27x + 4 \log_b \frac{3}{x}$$

as a single logarithm in its simplest form. [4]

- (c) Given that
- $\log_d 5 = \frac{1}{3}$
- , find the value of
- $d$
- . [2]

(C2 Summer 2018)

7. (a) Given that
- $x > 0$
- ,
- $y > 0$
- , show that

$$\log_a xy = \log_a x + \log_a y. \quad [3]$$

- (b) Find all values of
- $x$
- satisfying the equation

$$\log_a(11x^2 + 16x + 5) - \log_a(4x^2 + 1) = 3 \log_a 2. \quad [5]$$