

## Unit C2

### Pure Mathematics 2

Candidates will be expected to be familiar with the knowledge, skills and understanding implicit in Unit C1.

<b>Topics</b>	<b>Notes</b>
<p><b>1.</b> Sequences, including those given by a formula for the <math>n</math>th term and those generated by a simple relation of the form <math>x_{n+1} = f(x_n)</math>.</p> <p>Arithmetic series. The sum of a finite arithmetic series. The sum of the first <math>n</math> natural numbers.</p> <p>Geometric series. The sum of a finite geometric series. The sum to infinity of a convergent geometric series.</p>	<p>Use and proof of <math>S_n = \frac{n}{2}[2a + (n-1)d]</math> and <math>S_n = \frac{n}{2}[a + l]</math>.</p> <p>Use and proof of <math>S_n = \frac{a(1-r^n)}{1-r}</math>.</p> <p>Use of <math>S_\infty = \frac{a}{1-r}</math> for <math> r  &lt; 1</math>.</p> <p>The <math>\Sigma</math> notation.</p>
<p><b>2.</b> <math>y = a^x</math> and its graph.</p> <p>Laws of logarithms.  <math>\log_a x + \log_a y = \log_a (xy)</math>  <math>\log_a x - \log_a y = \log_a (x/y)</math>  <math>k \log_a x = \log_a (x^k)</math></p> <p>The solution of equations in the form <math>a^x = b</math>.</p>	<p>Use of the result that <math>y = a^x</math> implies <math>x = \log_a y</math>.</p> <p>Proof of the laws of logarithms.            Use of the laws of logarithms.            e.g. Simplify <math>\log_2 36 - 2\log_2 15 + \log_2 100</math>.</p> <p>Change of base will not be required.</p> <p>The use of a calculator to solve equations such as (i) <math>3^x = 2</math>,            (ii) <math>25^x - 4 \times 5^x + 3 = 0</math>.</p>

Topics	Notes
<p>3. Coordinate geometry of the circle using the equation of a circle in the form <math>(x - a)^2 + (y - b)^2 = r^2</math> (and in the form <math>x^2 + y^2 + 2gx + 2fy + c = 0</math>), and including use of the following circle properties:</p> <p>(i) the angle in a semicircle is a right-angle;</p> <p>(ii) the perpendicular from the centre to a chord bisects the chord;</p> <p>(iii) the perpendicularity of radius and tangent.</p>	<p>Equations of tangents. Condition for two circles to touch internally or externally. To include finding the points of intersection or the point of contact of a line and a circle.</p>
<p>4. The sine and cosine rules, and the area of a triangle in the form <math>\frac{1}{2} ab \sin C</math>.</p>	<p>To include the use of the sine rule in the ambiguous case. Use of the exact values of the sine, cosine and tangent of <math>30^\circ</math>, <math>45^\circ</math> and <math>60^\circ</math>.</p>
<p>Radian measure. Arc length, area of sector and area of segment.</p>	
<p>Sine, cosine and tangent functions. Their graphs, symmetries and periodicity.</p>	
<p>Knowledge and use of <math>\tan \theta = \frac{\sin \theta}{\cos \theta}</math> and <math>\cos^2 \theta + \sin^2 \theta = 1</math>.</p>	
<p>Solution of simple trigonometric equations in a given interval.</p>	<p>To include the solution of equations such as <math>3 \sin \theta = 1</math>, <math>\tan \frac{\theta}{2} = \sqrt{3}</math> and <math>2 \cos^2 \theta + \sin \theta - 1 = 0</math>.</p>
<p>5. Indefinite integration as the reverse of differentiation.</p>	
<p>Integration of <math>x^n</math> (<math>n \neq -1</math>).</p>	<p>Including sums, differences and polynomials.</p>
<p>Approximation of area under a curve using the trapezium rule. Interpretation of the definite integral as the area under a curve. Evaluation of definite integrals.</p>	<p>No consideration of error terms will be required in the examination. To include finding the area of a region between a straight line and a curve.</p>