

SJ: Cwestiynau Eraill

Graef 2007

⑤ (a)  $X \sim B(20, 0.35)$  Binomial  
(i)  $P(X=5) = {}^{20}C_5 0.35^5 (1-0.35)^{20-5}$   
 $= {}^{20}C_5 0.35^5 \times 0.65^{15}$   
 $= 0.1272$  i 4 lle degol

(Hefo Tablau:  $P(X=5) = P(X \leq 5) - P(X \leq 4)$   
 $= 0.2454 - 0.1182$   
 $= 0.1272.$ )

(ii)  $P(X < 8) = P(X \leq 7)$   
 $= 0.6010$  [Tablau]

(b) Blodau Melyn:  $Y \sim B(500, 0.03)$  Binomial  
Brasamcan Poisson:  $Y \sim Po(500 \times 0.03)$   
 $Y \sim Po(15)$

(i)  $P(Y=10) = \frac{15^{10} e^{-15}}{10!}$   
 $= 0.0486$  i 4 lle degol.

(Hefo Tablau:  $P(Y=10) = P(Y \leq 10) - P(Y \leq 9)$   
 $= 0.1185 - 0.0699$   
 $= 0.0486.$ )

(ii)  $P(Y > 12) = 1 - P(Y \leq 12)$   
 $= 1 - 0.2676$  [Tablau]  
 $= 0.7324.$

Haf 2007

$$\textcircled{3} \quad \begin{array}{ll} E(X) = 5 & \text{Var}(X) = 4 \\ E(Y) = 0 & \text{Var}(Y) = 1 \end{array}$$

$$Y = aX - b$$

Nawr  $E(Y) = aE(X) - b$

$$0 = a(5) - b$$

$$0 = 5a - b$$

$$\text{Var}(Y) = a^2 \text{Var}(X)$$

$$1 = a^2(4)$$

$$1 = 4a^2$$

$$4a^2 = 1$$

$$a^2 = \frac{1}{4}$$

$$a = \pm \sqrt{\frac{1}{4}}$$

$$a = \pm \frac{1}{2}$$

and mae  $a, b$  yn positif

felly  $a = \frac{1}{2}$

Felly  $0 = 5\left(\frac{1}{2}\right) - b$

$$\underline{b = 2\frac{1}{2}}$$

Haf 2010

$$\textcircled{2} \quad \begin{array}{ll} E(X) = 4 & \text{Var}(X) = 2 \\ Y = 3X - 1 \end{array}$$

(a)  $E(Y) = 3E(X) - 1$

$$E(Y) = 3 \times 4 - 1$$

$$E(Y) = 11$$

$$\text{Var}(Y) = 3^2 \text{Var}(X)$$

$$\text{Var}(Y) = 9 \times 2$$

$$\text{Var}(Y) = 18$$

(b)  $\text{Var}(Y) = E(Y^2) - [E(Y)]^2$

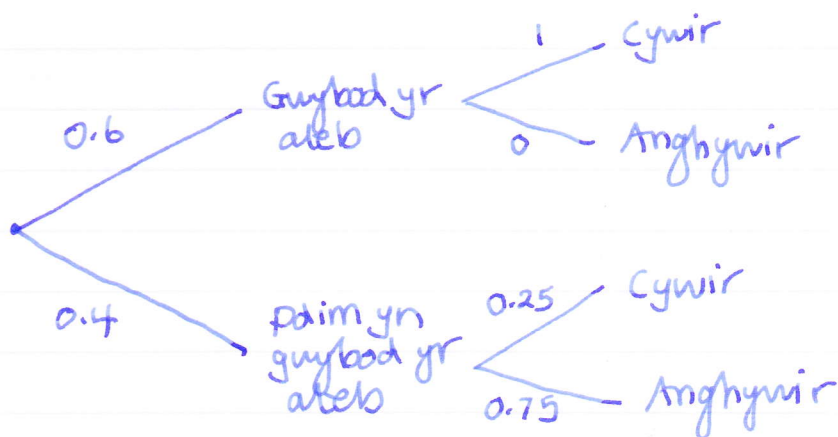
$$18 = E(Y^2) - 11^2$$

$$18 = E(Y^2) - 121$$

$$18 + 121 = E(Y^2)$$

$$E(Y^2) = 139$$

5



(a)  $P(\text{siôn yn rhoir ateb cywir})$   
 $= 0.6 \times 1 + 0.4 \times 0.25$   
 $= 0.6 + 0.1$   
 $= 0.7.$

(b)  $P(\text{Gwybod yr ateb cywir} \mid \text{Wedi ateb yn gywir})$   
 $= \frac{P(\text{Gwybod yr ateb cywir} \cap \text{Wedi ateb yn gywir})}{P(\text{Wedi ateb yn gywir})}$   
 $= \frac{0.6 \times 1}{0.7}.$   
 $= \frac{6}{7}.$

Haf 2012

② (a)  $E(X) = 8$   $\text{Var}(X) = 2$   
 $\text{Var}(X) = E(X^2) - [E(X)]^2$   
 $2 = E(X^2) - 8^2$   
 $2 = E(X^2) - 64$   
 $2 + 64 = E(X^2)$   
 $E(X^2) = 66$

(b)  $Y = 3X + 4$   
 $E(Y) = 3E(X) + 4$   
 $E(Y) = 3 \times 8 + 4$   
 $E(Y) = 28$   
 $\text{Var}(Y) = 3^2 \text{Var}(X)$   
 $\text{Var}(Y) = 9 \times 2$   
 $\text{Var}(Y) = 18$

SI Haf 2017

$$2) \quad E(X) = 10 \quad \text{Var}(X) = 2^2 \\ \text{Var}(X) = 4$$

$$a) \quad \text{Var}(X) = E(X^2) - [E(X)]^2 \\ 4 = E(X^2) - 10^2 \\ 4 + 100 = E(X^2) \\ E(X^2) = 104$$

$$b) \quad Y = 2X + 3$$

$$E(Y) = 2E(X) + 3$$

$$E(Y) = 2 \times 10 + 3$$

$$E(Y) = 23$$

$$\text{Var}(Y) = 2^2 \times \text{Var}(X)$$

$$\text{Var}(Y) = 4 \times 4$$

$$\text{Var}(Y) = 16$$