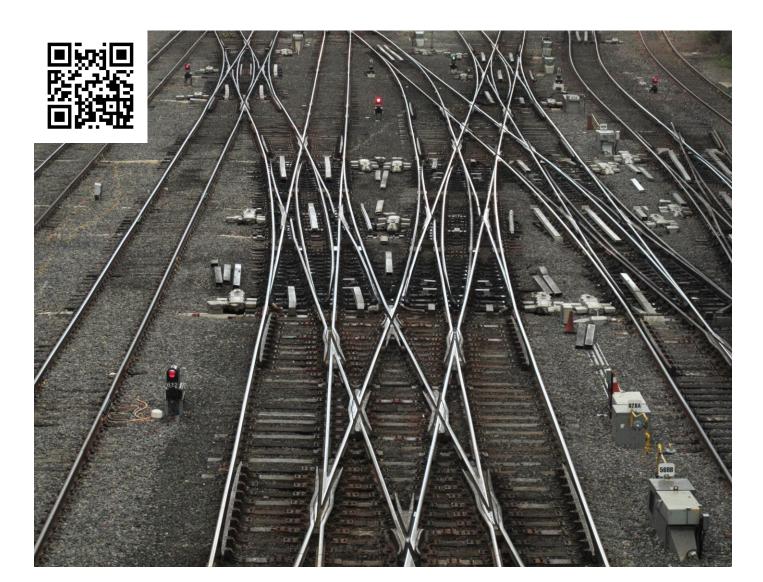




Chapter	Mathematics	Page Number
Directed Numbers	Ordering Directed Numbers. 'Less than' and 'More than'. Calculating with Directed Numbers (Addition; Subtraction; Multiplication; Division).	3
Decimals	 Adding and Subtracting Decimals. Multiplying and Dividing Decimals by a Whole Number Less Than 10. Ordering Decimals. Converting between Percentages and Decimals. Rounding Off to a Specified Number of Decimal Places. 	9
Angles 2	Revision of Year 7 work. Angles with Parallel Lines.	14
Transformations: Rotation	Rotating a Shape Around a Specific Point.	17



Directed Numbers

Numbers with a - sign before them are negative numbers.

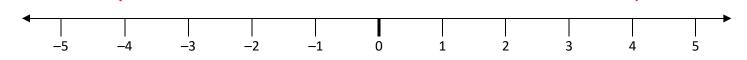
Other numbers (with the exception of zero) are **positive numbers**. Sometimes we write positive numbers with a + sign before them, e.g. **+5**.

Zero is neither positive nor negative.

We can show positive and negative numbers on a number line:

Negative direction; the numbers are decreasing

Positive direction; the numbers are increasing



Exercise 1

Write the following numbers in order, from least to greatest.

(a) 4 <i>,</i> –3 <i>,</i> 1 <i>,</i> –5 <i>,</i> 2	(b) –1, 4, 0, –2, 3
(d) –4, 7, –8, 9, –3	(e) 0, –12, 14, 1, –3
(g) 102, -94, -120, 96, -100	(h) 35, –42, 17, –54, 26
(j) –3, 5, –9, –1, 4	(k) –14, 17, –12, 13, –15

'Less than' and 'Greater than'

It is possible to write the symbols < or > between two different numbers. The symbol < means 'less than'. The symbol > means 'greater than'.

Example

7 is less than 10, so we can write 7 < 10. 3 is greater than -4, so we can write 3 > -4.

Exercise 2

Write the symbol < or > between the following pairs of numbers.

(a) 8 18	(b) 17 11	(c) 42	(d) 3 –5
(e) –2 –4	(f) –5 –1	(g) –3 0	(h) –4 2
(i) –5 –8	(j) 7 –8	(k) –102 <u>–</u> 98	(l) 14 –16
(m) –4 8	(n) –12 –3	(o) 87 165	(p) –87 –165

		;	
M	< ,	> .	? /
	₩ command	alt option	

The arrow always

points towards the **least** number.

Exercise 3

True or False?

(a) 8 > 5	(b) 3 > 9	(c) −4 > 2	(d)8 <5
(e) –10 > –7	(f) –4 < 8	(g) 9 > -14	(h) –21 > –19
(i) –12 < 10	(j) 180 < -190	(k) –120 > –90	(I) −4 < −3
(m) –4 > –7	(n) 0 < -4	(o) 8 > 0	(p) -9 > -11





Skill

Challenge! Search for "*Cool Cash Confusion*" on the internet. Write a short report on your findings.

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(c) -2, 4, -5, 5, 3

(f) -25, 27, -21, 29, -23 (i) -35, -32, -38, -37, -33 (l) 276, -156, 623, -312, 76

Exercise 4

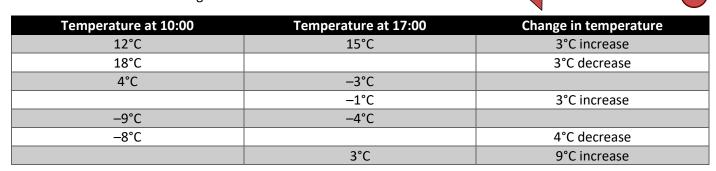
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Applying

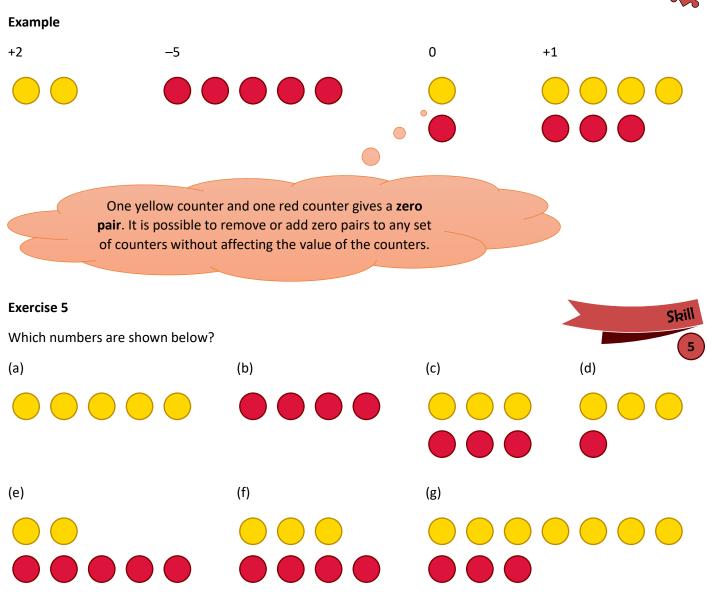
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Fill in the blanks in the following table.



Calculating with Directed Numbers

Two sided counters have a yellow face and a red face. The yellow face represents +1 (positive one) and the red face represents -1 (negative one).



Ysgol y Creuddyn			Th	e Mathematics Department
Speaking Sums				
Example				
3 + -2	3 – –2		-32	
'Three add negative two	' 'Three subti	ract negative two'	'Negative three su	btract negative two'
Exercise 6				5
Write down how you wo	ould say the followin	g sums.		
(a) 8 + 2 (e) 8 + -2	(b) 8 – 2 (f) 8 – –2		(c) -8 + 2 (g) -8 + -2	(d) -8 - 2 (h) -82
			dition or subtraction sum	
Example				
3 + -2	3 – –2		-32	
Start with 3 yellow coun	ters Start with 3	yellow counters	Start with 3 red co	unters
		•		
Add 2 red counters	Add 2 zero j	pairs (Why?)	Subtract two red co	ounters
Remove any zero pairs	Subtract tw	o red counters	Count what is left:	-1
Count what is left: 1	Count what	is left: 5		
Exercise 7				
Use two sided counters	to answer the follow	ving sums.		
(e) –5 + 2 (i) 2 + 5	(b) 5 – 2 (f) 5 – –2 (j) 2 – 5 (n) –2 – 5	(c) 5 + -2 (g) -52 (k) -2 + 5 (o) -25	(d) -5 + -2 (h) -5 - 2 (l) -2 + -5 (p) 25	
Exercise 8				
Use two sided counters	to answer the follow	ving sums.		
(a) 6 + -4	(b) 7 + -3	(c) $5 + -3$	(d) $6 + -1$	

(a) 6 + -4(b) 7 + -3(c) 5 + -3(d) 6 + -1(e) -6 + -4(f) -7 + -3(g) -5 + -3(h) -6 + -1

(i) Complete the following sentence: Adding a negative number is the same as ______.

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Use two sided counters to answer the followin	g sums.
---	---------

(a) 4 – –3	(b) 3 – –4	(c) 5 − −2	(d) 1 – –7
(e) -43	(f) -34	(g) −5 − −2	(h) –1 – –7

(i) Complete the following sentence: Subtracting a negative number is the same as ______.

Adding and Subtracting Negative Numbers

-				1		1	1	-			- T				•	1	-	1	1	-	-		1		1	-			→
						-									-							-							
	-1	.2 –1	1 –1	10 –	9-	-8	-7	-6	-5	-4	-3	3 –	2 –	-1	0	1	2	3	4	5	6	7	8	3 9	9	10	11	12	<u>'</u>
	_				-	-	-	-	-	-	-		_	-	-	_	_	-	-	-	-	-		-	-				-

Example

(a) 9 + -2 = 9 - 2	(b) -4 + -3 = -4 - 3	(c) 7 – –2 = 7 + 2	(d) -41 = -4 + 1	
= 7	= -7	= 9	= -3	
Exercise 10				
(a) 4 + -2	(b) 10 + -2	(c) 9 + -4	(d) 2 + -9	
(e) -5 + -2	(f) -9 + -2	(g) -3 + -3	(h) -1 + -7	
(i) 6 + -8	(j) 2 + -5	(k) 9 + -11	(l) 7 + -7	
(m) -14 + -3	(n) -18 + -8	(o) -24 + -8	(p) -38 + -5	
Exercise 11				
(a) 6 – –4	(b) 84	(c) 13	(d) 45	
(e) –8 – –2	(f) -73	(g) -29	(h) -62	
(i) –2 – –5	(j) -48	(k) -12	(l) -88	
(m) –20 – –5	(n) -217	(o) 148	(p) -1014	
Exercise 12				
(a) $8 + -3$	(b) 83	(c) $-8 + -3$	(d) -83	
(e) 142	(f) 214	(g) $14 + -2$	(h) $2 + -14$	
(i) $-7 + -9$	(j) -79	(k) $-9 + -7$	(l) -97	
(m) 242	(n) $-12 + -2$	(o) -912	(p) $3 + -8$	
(q) $2.5 + -0.3$	(r) $5.41.2$	(s) $-2.10.5$	(t) $-4.2 + -0.7$	
(u) $25 + -2 + -3$	(v) $25 + -23$	(w) 2523	(x) $252 + -3$	

Challenge!

What should the answers be to the following?

(a) 16 + +4 (b) 16 - +4

(c) 1 + -2 - -3 + -4 - -5



Exercise 13

(a) In a golf championship, players complete four rounds of golf on the golf course. Out of the following four players, who has the best score? (In golf, the lower the score, the better the score.)

Name	Round 1	Round 2	Round 3	Round 4
Jordan Speith	+2	-3	-1	+1
Rickie Fowler	-2	-1	+4	-3
Rory McIlroy	0	-3	+1	-2
Justin Rose	-3	+2	+4	-2

Remember! The

ttrockstars

website will

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(b) The temperature at midnight in Llanrwst was recorded each day during one week in January.

Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday
-3°C	−4°C	1°C	−3°C	−2°C	0°C	4°C

What was the mean temperature at midnight in Llanrwst during this week?

(c) At the end of May, Trefor had £200 in his bank account. He spent £800 during the first week of June. He was paid £500 during the second week of June. In the third week, he spent £400. During the final week of June, he was paid £900. How much money has Trefor got in his bank account at the end of June?

17

(c) 3 × 8

(g) 4 × 7

(k) 8 × 9

(o) 8 × 11

Multiplying and Dividing Directed Numbers

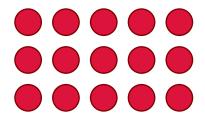
Exercise 14 (Revision)

(a) 5 × 6	(b) 7 × 2
(e) 9 × 4	(f) 2 × 9
(i) 8 × 7	(j) 9 × 6
(m) 5 × 9	(n) 12 × 6

Multiplying Directed Numbers

What is $3 \times -5?$

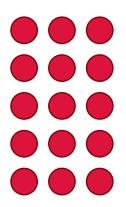
We can think of 3×-5 as 'three lots of negative five', which is three rows of five red counters. We can see from the diagram below that this gives -15. So, $5 \times -3 = -15$.



In general, multiplying a positive number by a negative number gives a negative answer.

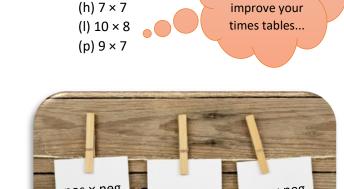
What is -3×5 ?

The order in which we multiply numbers is not important, so we can think of -3×5 as 5×-3 , which is five rows of three red counters. We can see from the diagram below that this gives -15. So, $-3 \times 5 = -15$.



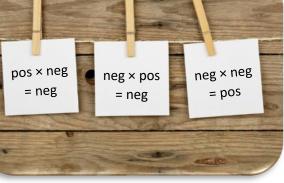
In general, multiplying a negative number by a positive number gives a negative answer.





Skill

(d) 6 × 7



What is
$$-3 \times -5$$
?

-3 × -5 = -1 × 3 × -5	Write the -3 as -1×3
= -1 × -15	Calculate $3 \times -5 = -15$
= 15	Multiplying by –1 changes the sign of the number / changes the colour of the counters

In general, multiplying a negative number by a negative number gives a positive answer.

Example

(a) 8 × −3 = −24	(b) –4 × 5 = –20	(c) −6 × −2 = 12
Exercise 15		

(a) 7 × –3	(b) –3 × 7	(c) −3 × − 7	(d) −7 × −3
(e) 4 × –8	(f) −2 × 6	(g) −4 × −6	(h) 6 × –8
(i) –9 × 3	(j) −7 × −5	(k) −9 × −4	(I) −5 × 8
(m) 11 × –2	(n) 4 × 12	(o) –9 × 6	(p) –8 × 7
(q) -8 × -8	(r) 12 × –6	(s) –7 × 9	(t) –5 × –9
(u) 13 × –3	(v) –1 × 10	(w) –8 × 0	(x) −1 × −1
(y) 9 × –8	(z) −14 × −3	(α) –6 × 5	(β) 15 × –6

Exercise 16

Evaluate the answers to the following. Use your calculator to check your answers.

(a) 8 + –5	(b) 8 <i>——</i> 5	(c) 8 × –5	(d) –8 × –5
(e) −4 + −2	(f) -42	(g) −4 × −2	(h) –4 × 2
(i) 14 × −2	(j) 14 + -2	(k) –14 + –2	(I) −14 − −2
(m) 4 – –9	(n) –4 + –9	(o) –4 × 9	(p) 4 × –9

Exercise 17

Write 10 different sums whose answer is 4.

Dividing Directed Numbers

The rules for dividing directed numbers are the same as for multiplication. These rules are shown in the diagram on the right.

Example

(a) 32 ÷ 4 = 8	(b) 32 ÷ −4 = −8
(c) −32 ÷ 4 = −8	(d) -32 ÷ -4 = 8

Exercise 18

(a) 16 ÷ −2	(b) −24 ÷ 4	(c) −12 ÷ −3
(e) 28 ÷ −4	(f) -30 ÷ 2	(g) 36 ÷ –9
(i) 48 ÷ −6	(j) 50 ÷ –25	(k) -39 ÷ -13
(m) 66 ÷ –2	(n) –72 ÷ 8	(o) 63 ÷ -7
(q) –100 ÷ 20	(r) −120 ÷ −40	(s) 2 ÷ –4
(u) −125 ÷ −5	(v) 1000 ÷ 100	(x) −1 ÷ −10



5

(d) –20 ÷ –5
(h) -40 ÷ -10
(I) 64 ÷ −8
(p)80 ÷8
(t) 0 ÷−3
(y) –7 ÷ 0



Calculate the following. (Be careful with the order of operations.)

(a) 8 + 2 × −3	(b) 8 − 2 × −3	(c) −8 × 2 − 3	(d) −8 ÷ −2 − −3
(e) 3 + 6 ÷ −3	(f) −3 + −6 ÷ 3	(g) 3 × 6 ÷ −3	(h) −3 + −6 − −3
(i) (4 + −2) × −5	(j) 4 + (−2 × −5)	(k) 4 + −2 × −5	(l) (5 × –6) ÷ (–20 ÷ 5)

Exercise 20

Calculate the following.

Complete the following tables.

(a) 2 ²	(b) (-2) ²	(c) 2 ³
(e) 2 ⁴	(f) (-2) ⁴	(g) 2 ⁵
(i) (-1) ²	(j) (-1) ³	(k) (-1) ⁴

Exercise 21

×	3	-6	
4	12		-32
	6		
5			
-10			

÷	2	-4	
16	8		2
	16		
-16			
48			

(d) (-2)³ (h) (-2)⁵ (l) (-1)⁵⁰

Exercise 22 (Revision)

(a) Write the following numbers in order, from least to greatest.

(i) 8, -2, -10, 5, 7(ii) -3, 6, -5, 8, -7, 0(iii) 23, -21, 18, 25, -4, -12, 8, -1, 3, -19(b) Write the symbol < or > between the following pairs of numbers.(i) $-3 _ 2$ (ii) $-8 _ -4$ (iii) $-15 _ 12$ (c) 8 + -2(d) 14 - -3(e) 2×-3 (f) $-14 \div -2$ (g) -8 + -2(h) -14 - -3(i) -2×-3 (j) $14 \div -2$

(k) Copy and complete the following sentences.

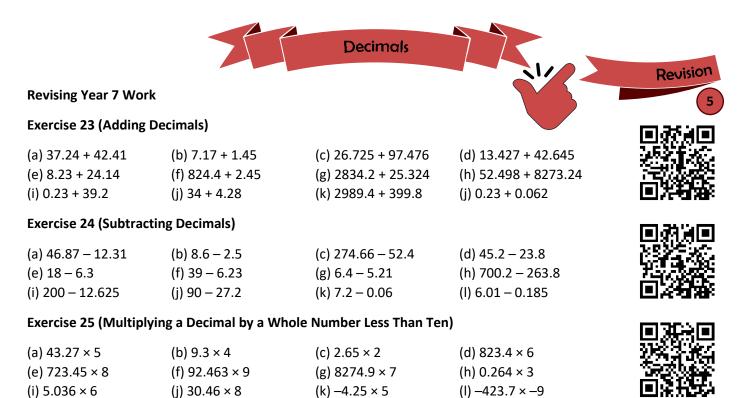
(i) Adding a negative number is the same as ______ (ii) Subtracting a negative number is the same as ______

(iii) Multiplying a negative number by a positive number gives an answer that is _____

(iv) Dividing a negative number by a negative number gives an answer that is _____



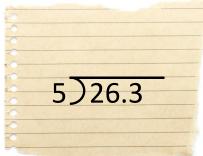
Key Words	Corrections	I am happy with	I need to revise



Dividing a Decimal by a Whole Number Less Than Ten

In order to calculate a sum such as $26.3 \div 5$, follow these steps.

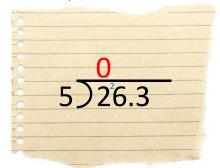
1. Set the sum out using a division frame; the 26.3 goes inside and the 5 goes outside.



4. Remember to add the decimal point in the correct position.



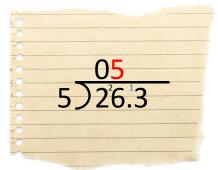
2. "How many times does 5 fit into 2?" 5 is too big to fit into 2, so it fits in 0 times, with remainder 2.



5. "How many times does 5 fit into 13?" It fits into thirteen 2 times, with remainder 3. Note that we need to write an extra 0 before writing the remainder.



3. "How many times does 5 fit into 26?" It fits into twenty-six 5 times, with remainder 1.



6. "How many times does 5 fit into 30?" It fits into thirty 6 times, with remainder 0. So, the answer to 26.3 ÷ 5 is 5.26.



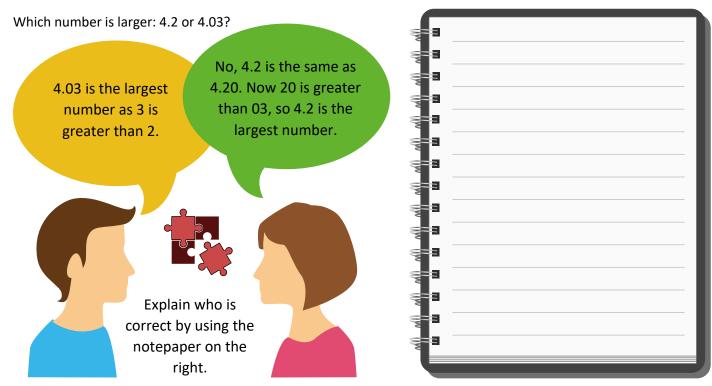
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Skill

Exercise 26

(a) 7.35 ÷ 3	(b) 26.88 ÷ 4	(c) 842.6 ÷ 2	(d) 213.5 ÷ 5	5
(e) 252.6 ÷ 6	(f) 75.6 ÷ 9	(g) 341.84 ÷ 8	(h) 29.61 ÷ 7	
(i) 2531.1 ÷ 6	(j) 72.32 ÷ 8	(k) 186.06 ÷ 3	(l) 371 ÷ 5	
(m) 0.85 ÷ 2	(n) 297 ÷ 4	(o) 37941.75 ÷ 9	(p) 305.004 ÷ 7	

Ordering Decimals



Exercise 27

Write the following numbers in order, from least to greatest.

(a) 4.2, 4.02, 4.03, 4.3
(d) 9.008, 9.8, 9.08, 9
(g) 0.26, 0.18, 0.3, 0.21, 0.33
(j) 0.9, 0.78, 0.98, 0.09, 0.87
(m) 5.9, 6.8, 5.09, 5.83, 6.88

(b) 8.42, 2.84, 4.82, 8.24, 4.28, 2.48
(e) 3.96, 3.09, 3.6, 3.06, 3.096, 3.009
(h) 3.8, 3.07, 4.09, 3.54, 4.81, 3.05
(k) 0.821, 0.281, 0.128, 0.218, 0.812
(n) 1.8, 1.03, 1.24, 1.043, 1.003, 1.51

(c) 7.503, 7.053, 7.53, 7.005, 7.3
(f) 14.07, 4.71, 7.14, 14.1, 7.04, 4.07
(i) 23.7, 20.3, 21.78, 20.09, 22.7
(l) 0.7, 0.68, 0.702, 0.689, 0.73, 0.679
(o) 45.08, 5.8, 45.8, 5.004, 45.50, 5.08

Exercise 28

	Runner 1	Runner 2	Runner 3	Runner 4
Canada	10.31 seconds	10.04 seconds	10.46 seconds	10.09 seconds
Jamaica	9.98 seconds	10.68 seconds	10.10 seconds	10.18 seconds
U.S.A.	10.06 seconds	10.13 seconds	10.24 seconds	10.01 seconds
France	10.53 seconds	10.96 seconds	10.42 seconds	10.18 seconds

The table above shows the times taken by each runner in a 400 m relay race at an athletics championship.

- (a) How many different teams were competing?
- (c) Which runner, from which team, was fastest?
- (e) Which team won the relay race?

- (b) How many runners were in each team?
- (d) Which runner was slowest?
- (f) Which team came last?



Applying

Add some of the following decimals, aiming to reach a total as close as possible to 1. You may only use each number once.



Converting a Percentage to a Decimal

In order to change a percentage to be a decimal, divide the percentage by 100.

Example

(a) As a decimal, 62% is 62 ÷ 100 = 0.62.

(b) As a decimal, 3% is 3 ÷ 100 = 0.03.

Exercise 30

Write the following percentages as decimals.

(b) 86%
(f) 8%
(j) 250%
(n) 4.7%

(d) 35% (h) 2% (I) 0% (p) 0.08%



Converting a Decimal to a Percentage

In order to change a **decimal** to be a **percentage**, multiply by 100 and add the % symbol.

(c) 29%

(g) 70%

(k) 400%

(0) 0.3%

Example

(a) As a percentage, 0.45 is $0.45 \times 100 = 45\%$.

(b) As a percentage, 0.06 is $6 \times 100 = 6\%$.

Exercise 31

Write the following decimals as percentages.

(a) 0.31	(b) 0.57	(c) 0.73	(d) 0.66
(e) 0.2	(f) 0.9	(g) 0.04	(h) 0.09
(i) 3.54	(j) 5.5	(k) 6	(I) 12
(m) 0.728	(n) 0.035	(o) 0.002	(p) 0.0006

Exercise 32

Write the following numbers in order, starting from the smallest.

54% 0.35 7% 0.09 2.1 92% 0.8 40%



Rounding Off to a Specified Number of Decimal Places

Exercise 33

Complete the following table.



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Original Number	Round off to the nearest unit	Round off to the nearest 10	Round off to one decimal place	Round off to two decimal places	Round off to three decimal places
432.4385	432	430	432.4	432.44	432.439
273.8924					
348.8753					
219.5541					
199.7502					
537.8025					
1,549.1087					
3,845.6355					
10,293.54					
28,479.5997					

Exercise 34 (Revision)

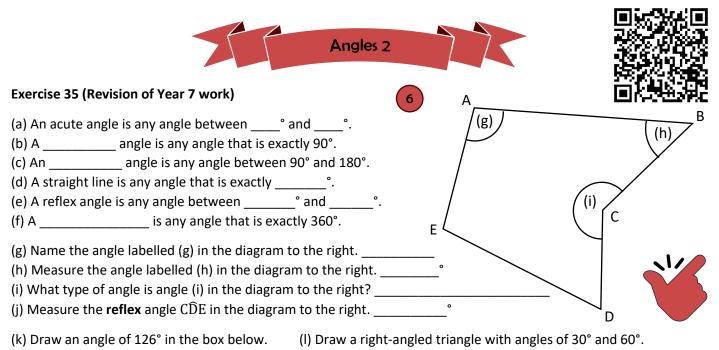
(a) 154	1.2 + 87.9	9	(b) 275	.3 – 184	.9		(c) 835.	6 × 7	(d) 145.8 ÷ 6
(e) Wr	ite the fo	ollowing	g number:	s in orde	er, from	least to	greatest.		
4.1	3.05	3.5	3.124	4.12	4.214	3.99			
(f) Cha	(f) Change the following percentages to be decimals.								
(i) 34%	D		(ii) 8%				(iii) 81%	0	(iv) 0.4%
(g) Round off the number 283.4672									
(i) to o	ne decir	nal plac	е	(ii) to t	wo decir	nal plac	es	(iii) to three de	cimal places.

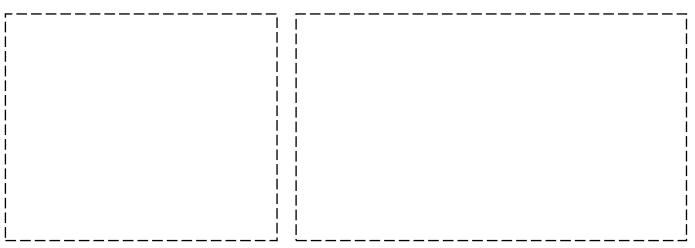


Key Words	Corrections	I am happy with	I need to revise

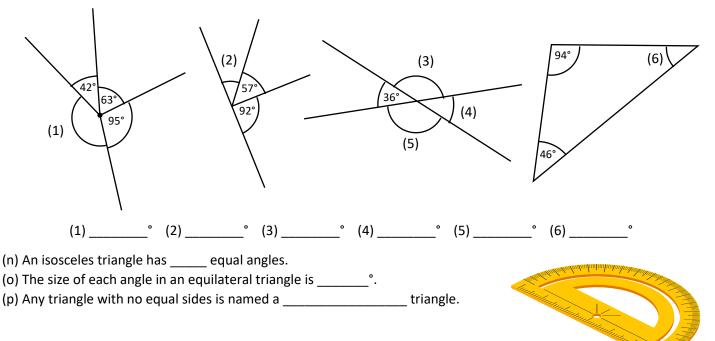
6

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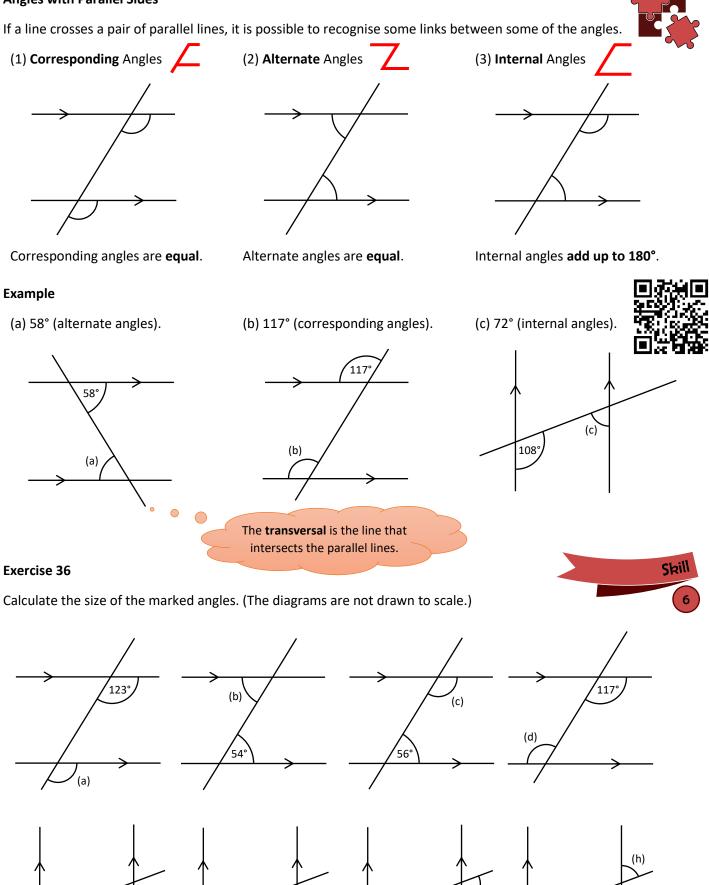




(m) Calculate the size of the angles in the following diagrams. (The diagrams are not drawn to scale.)



Angles with Parallel Sides



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105

(e)

72

(f)

113

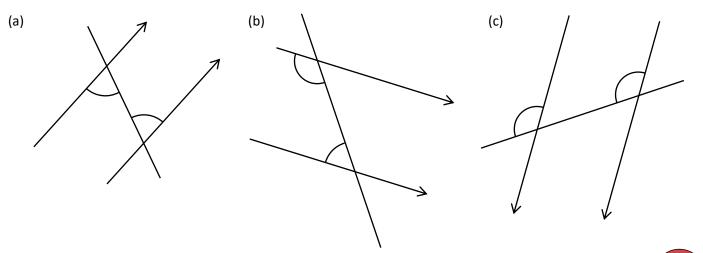
(g)

68°

6

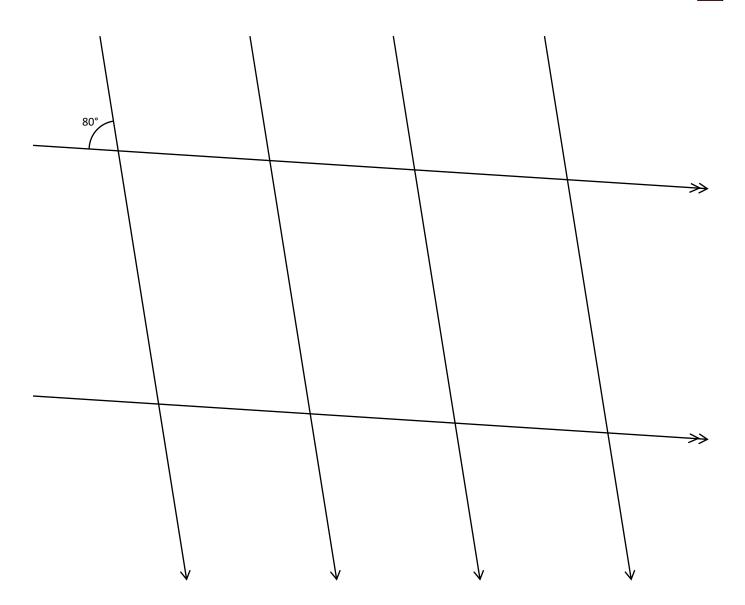
Exercise 37

Are the following pairs of angles corresponding angles, alternate angles or internal angles?



Exercise 38

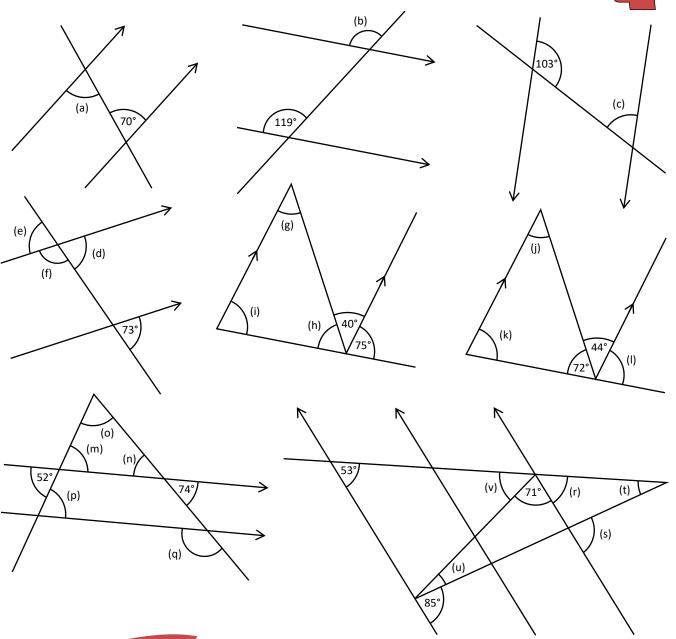
Find as many angles as you can in the following diagram. (The diagram is not drawn to scale.)



6

Exercise 39

Calculate the size of the marked angles. (The diagrams are not drawn to scale.)





Key Words	Corrections	I am happy with	I need to revise

The Mathematics Department



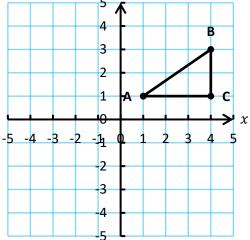
Rotation is one of the four transformations.

Year 7	Year 8	Year 9	Year 10
Translation	Rotation	Reflection	Enlargement
In order to rotate a s	hape, we need to kr	now	3 to the right,
	f rotation , e.g. the p e the shape, e.g. 90°		5 up
			e a rotation question.

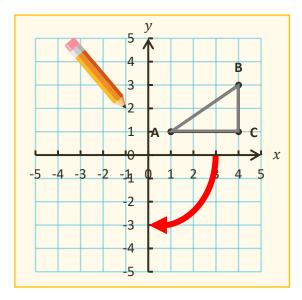
Transformations: Rotation



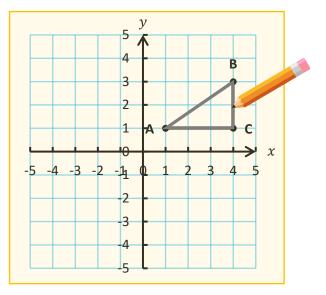
Example: Rotate the triangle ABC by 90° clockwise around the point (-1, 2). $5 \frac{y}{5}$



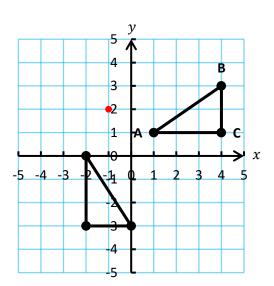
Step 2: Place your pencil on the centre of rotation (-1, 2) and rotate the tracing paper 90° clockwise.



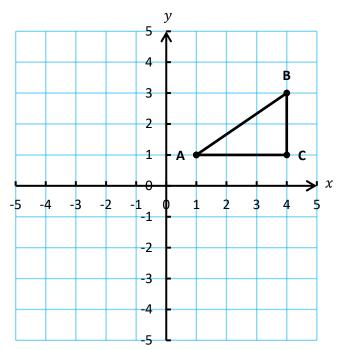
Step 1: Place a piece of tracing paper over the grid and trace the shape **ABC**.



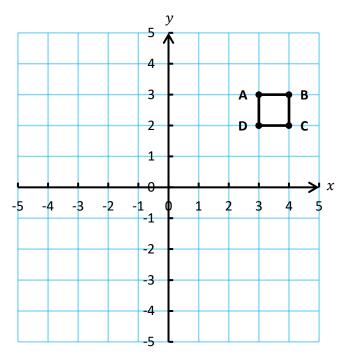
Step 3: Draw the new shape on the squared paper.



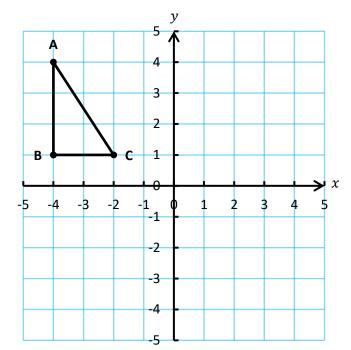
(a) Rotate the triangle **ABC** by 90° clockwise around the origin.



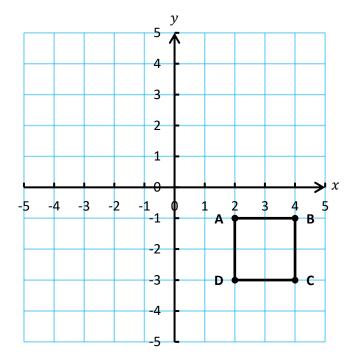
(c) Rotate the square **ABCD** by 180° clockwise around the origin.



(e) Would the answer to question (c) change if the word "clockwise" was changed to the word "counter-clockwise"? (b) Rotate the triangle **ABC** 6 by 90° counter-clockwise around the origin.

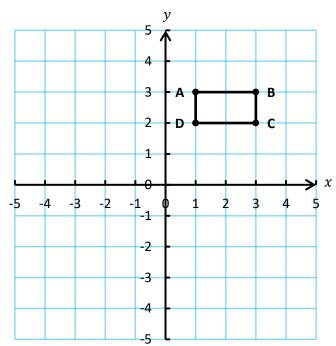


(d) Rotate the square **ABCD** by 270° counter-clockwise around the origin.

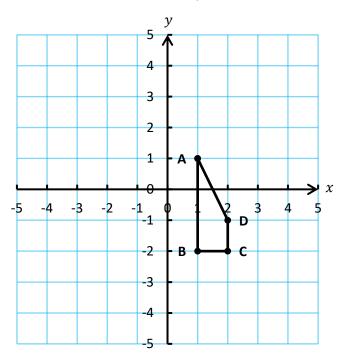


(f) Complete the sentence: a counter-clockwise rotation of 270° is the same as a clockwise rotation of _____°.

(a) Rotate the rectangle ABCD by 90° clockwise around the point (-1, 2).

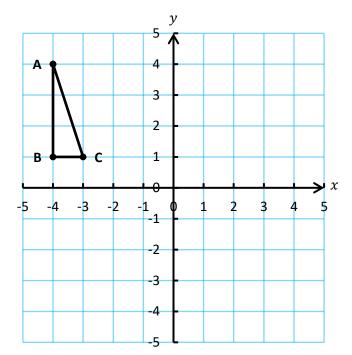


(c) Rotate the quadrilateral ABCD by 90° counter-clockwise around the point (0, 1).

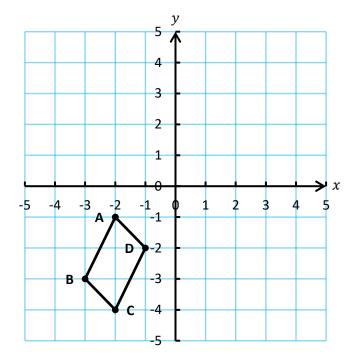


- Give your answer in square units.

- 6
- (b) Rotate the triangle ABC by 180° counter-clockwise around the point (-2, 2).



(d) Rotate the quadrilateral ABCD by 270° counter-clockwise around the point (2, -4).

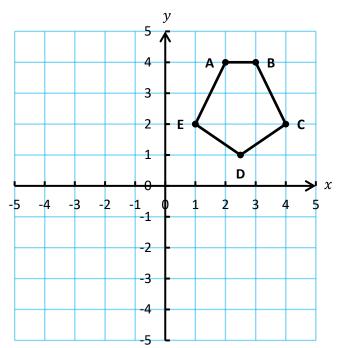


- (e) What is the name of the quadrilateral in question (c)? (f) What is the name of the quadrilateral in question (d)?
- (g) Calculate the area of the quadrilateral in question (c). (h) Calculate the area of the quadrilateral in question (d). Give your answer in square units.

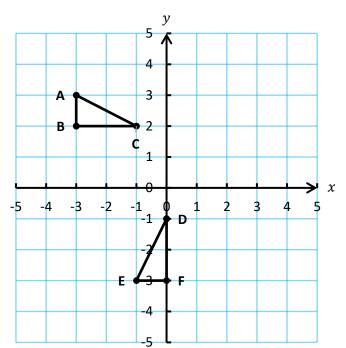
6

Exercise 42

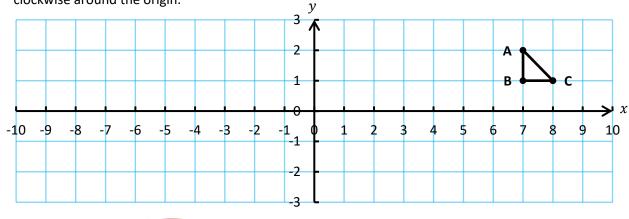
(a) Rotate the pentagon **ABCDE** by 90° clockwise around the point (-1, 1).



(b) What **type** of rotation changes the triangle **ABC** to the triangle **DEF**?



(c) First, translate the triangle **ABC** using the column vector $\begin{pmatrix} -5 \\ -1 \end{pmatrix}$. Then, rotate the translated triangle by 90° clockwise around the origin.





Key Words	Corrections	I am happy with	I need to revise

The End Reflection Sheet				
of Year 8 Name: Percentage in the test:	I know this.	I need to revise this.	Question in the test:	Correct in the test?
I know how to order positive and negative numbers from least to greatest.			2, 7	
I know when to write the symbols < or > between a pair of numbers, e.g. 5 > –8.			3	
I can add negative numbers , e.g. 3 + –9.			4	
I can subtract negative numbers , e.g. 4 − −7.			4	
I can multiply and divide by directed numbers, e.g. 4×-5 , $-20 \div -10$.			4	
I can add, subtract and multiply using decimals , e.g. 37.24 + 42.41, 14 – 4.21, 45.65 × 6.			5, 6, 8	
I can divide a decimal by a whole number less than 10 , e.g. 75.6 ÷ 9.			6	
l can change a percentage into a decimal .			9	
l can change a decimal into a percentage .			10	
l can round off a number to a specified number of decimal places.			1	
Given parallel lines, I can recognise and use corresponding angles, alternate angles and internal angles.			11	
I can rotate a shape around a specified point .			12, 13	